Dynamic Extension of Starling Resistor Model

A. Mikuckas, A. Venckauskas
Department of Computer Science, Kaunas University of Technology,
Studentu str. 50, LT-51368 Kaunas, Lithuania, phone: +370 300 395, e-mail: antanas.mikuckas@ktu.lt

I. Mikuckiene
Department of System Analysis, Kaunas University of Technology,
Studentų str. 50, LT-51368 Kaunas, Lithuania

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Introduction

Biotronics technology is widely used for the investigation and management of biological systems. The main objectives for such systems were formulated in [1]. Medical electronics evolves toward intelligent interactive systems [2], it is necessary to ensure the effectiveness of such systems [3]. This requires adequate models of physiological processes. These models of the cardiovascular system are based on lumped parameter description using the electrical analogue of cardiovascular systems [4]. In computational models voltage corresponds to pressure, current to flow, capacitance to elastic properties and inductance to inertial properties. The resistance simulates the resistance of flow encountered by the blood as it flows from the major arteries to minor arteries and capillaries due to decreasing vessel diameter. Particular segments of vessels are described by Windkessel models. These models are linear – values of resistance, capacitance and inductance are constant.

Tissue pressure increases in the case of a stroke or trauma. In areas with increased tissue pressure the linear models are unsuitable.

Static Starling resistor model

The Starling resistor describes vascular beds with increased compartment pressure [4, 5]. The blood flow $Q$ in the vessel is determined by the relationships between inflow pressure $P_I$, external pressure $P_E$ and outflow pressure $P_V$. There are three West zones [6] where these relationships are defined. In zone 1 ($P_E > P_I > P_V$) blood flow $Q$ equals zero. In zone 2 ($P_I > P_E > P_V$) $Q$ is proportional to $(P_I - P_E)$. In zone 3 ($P_I > P_V > P_E$) $Q$ is proportional to $(P_I - P_V)$.

In the case of compartment injury, there are tissue pressure gradients from the centre to the periphery of focal injury. As a result, different West zones exist in the same vascular network. This will cause blood flow diversion via the pathway of least resistance. This blood flow redistribution in veins is called “cerebral venous steal” [7]. Starling’s model is a model for the investigation of the effects of tissue pressure differences on blood flow. It is considered that increased venous pressure may increase blood flow to regions with increased tissue pressure and prevent secondary injury from the venous steal.

The concept of blood flow redistribution with increased venous pressure was verified by the static Starling resistor model. A constant blood pressure is used in this model; this may cause errors in estimations.

A segment of vascular system with increased tissue pressure is depicted (Fig 1).
Fig. 2. The electrical analogue of vascular system segment

In this model resistors $R_{S1}$ and $R_{S2}$ are Starling resistors which value depend on pressures $P_K, P_E$ and $P_L$:

$$R_S = \begin{cases} R_0 \frac{P_K}{P_E}, & P_L - P_E > P_L, \\ \infty, & P_L - P_E \leq P_E. \end{cases}$$ (1)

In the electrical analogue of vascular system segment $U$ corresponds to pressure $P_K$, $U_5$ corresponds to pressure difference ($P_L - P_E$). The values of resistors $R_{S1}$ and $R_{S2}$ may be different tissue values $E_1$ and $E_2$ ($E$ in electrical analogue of vascular system corresponds to tissue pressure $P_E$)

$$R_{Sj} = \begin{cases} R_0 U_j, & U_j > E_j, \\ U_j - E_j, & U_j \leq E_j, \ j = 1,2. \end{cases}$$ (2)

When the blood vessel bifurcates two cases are possible:
- $E_1 >> E_2$, or $E_1 << E_2$. In this case there is no blood flow in the vessel with a higher tissue pressure;
- $E_1 \approx E_2$. In this case:

$$U_S = \frac{U(t) R_0 R_{01} + R_0 R_{10} E_1 + R_0 E_2}{R_0 R_{01} + R_0 R + R_0 R},$$ (3)

$$I_{S1} = \begin{cases} \frac{U(t) R_0 - E_1 (R_0 + R) + E_2 R}{(R_0 + R) R_0}, & U(t) > E_1, \\ 0, & U(t) \leq E_1, \end{cases}$$ (4)

$$I_{S2} = \begin{cases} \frac{U(t) R_0 - E_2 (R_0 + R) + E_1 R}{(R_0 + R) R_0}, & U(t) > E_2, \\ 0, & U(t) \leq E_2. \end{cases}$$ (5)

Experiments

We have built two static models in MATLAB and its supplement SIMULINK. The input signal $U(t)$ for the first model is blood pulse. This curve can be divided to two parts; the first part represents cardiac tissue in systole and can be approximated by sine wave and the second part of the input curve is equal to zero

$$U(t) = \begin{cases} U \sin^2 \left( \frac{\pi \cdot t}{T_s} \right), & t \in (0, T_s), \\ 0, & t \in \left[ T_s, T \right). \end{cases}$$ (6)

The input signal is depicted in Fig. 3.

The input signal for the second model is constant voltage $U$ (corresponds to constant pressure $P_L$). The second model corresponds to the model represented in [5]. Other parameters in both models: $R_0 = 30, R = 85, U = 1$.

These values of parameters are chosen in order to compare modelling results with results represented in [5]. The modelling results are depicted in Fig. 4 and Fig. 5, where

$$S_1 = \frac{I_1}{I_1 + I_2}, \quad S_2 = \frac{I_2}{I_1 + I_2}. \quad (7)$$

Fig. 3. The input signal of model

Fig. 4. The blood flow distribution when blood vessel bifurcates:
- a – model with constant pressure; b – model with blood pulse. Tissue pressure $E_i = 0, E_2 = 0.2$

The blood flow improvement in blood vessels with increased tissue pressure is less noticeable when the first model is used.

The case where tissue pressure gradient is small is depicted in Fig. 5.

Fig. 5. The blood flow distribution when blood vessel bifurcates:
- a – model with constant pressure; b – model with blood pulse. Tissue pressure $E_i = 0, E_2 = 0.2$
The blood flow distribution when blood vessel bifurcates: a – model with constant pressure; b – model with blood pulse. Tissue pressure $E_1 = 0.1$, $E_2 = 0.13$

In the case where the difference of tissue pressure value is not large, modelling results differ significantly. The elevation of pressure in a certain range does not restore blood flow.

The results of the model with blood pulse are more precise because the blood flow redistribution occurs only during the time period when pressure of blood pulse exceeds some threshold.

Dynamic model

The electrical analogue of a cardiovascular segment is depicted in Fig. 6. The model includes two Starling resistors with common inflow and a capacitance. Starling resistors evaluate tissue pressure and capacitance evaluates blood vessel elastic properties.

In this model we must solve the following equations:

$$\frac{dU_C}{dt} = \frac{U_C}{C} \left( 1 + \frac{1}{R} + \frac{1}{R_{S2}} \right) \frac{U}{RC},$$

$$R_{S1} = \begin{cases} \frac{R_0 U_C}{U_C - E_1}, & U_C > E_1, \\ \infty, & U_C \leq E_1, \end{cases}$$

$$R_{S2} = \begin{cases} \frac{R_0 U_C}{U_C - E_2}, & U_C > E_2, \\ \infty, & U_C \leq E_2. \end{cases}$$

We have built a dynamic model in MATLAB and its supplement SIMULINK. The main subsystem of this model is depicted in Fig. 7.

The input signal is the same as in the first static model. It is possible to change tissue pressure values $E_1$, $E_2$ and to use various resistors $R_0$ for different blood vessels.

The modelling results in Fig. 8 show that increased blood pressure does not restore blood flow misdistribution efficiently when tissue pressure gradient is high.

The case when tissue pressure gradient is low is depicted in Fig. 9.

This possibility is very important for modelling more complex cardiovascular subsystems.

The results of a modelling are depicted in Fig. 8.

In this case parameters $S1$ and $S2$ are

$$S1 = \frac{I_{11}}{I_{11} + I_{21}}, \quad S2 = \frac{I_{21}}{I_{11} + I_{21}},$$

where

$$I_{11} = \frac{T}{T_0} \int I_1(t) dt, \quad I_{21} = \frac{T}{T_0} \int I_2(t) dt.$$
When the tissue pressure difference is low, elevated pressure restores the blood flow more effectively. In some range of blood pressure the ratio of the flow in the vessels 1 and 2 increases. When blood pressure exceeds a certain threshold (depending on tissue pressure) then blood flow ratio decreases.

Conclusions

The development of intelligent medical systems, electronic monitoring systems required for physiological models. The blood pressure support biomedical devices need a model of the cardiovascular system.

The Starling resistor static model does not evaluate blood vessels elastic properties, so blood flow redistribution with elevation of pressure is overrated.

The Starling resistor dynamic model is more precise and allows fixing the blood pressure threshold when the blood flow improvement in a blood vessel with increased tissue pressure occurs. This threshold is less expressed in static model. The threshold fixing is very important by creating the real-time blood pressure support biomedical devices, because too high pressure may be harmful.

References


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The development of intelligent medical systems, electronic monitoring systems required for physiological models. The proposed model of venous blood flow realized on the electric circuit basis can be used to support the development of blood pressure, real-time devices. Designed for venous blood nonlinear dynamic model is an extension of Starling resistor model. When the tissue pressure increased, static models are not suitable. Suggested non-linear dynamic model allows determining the threshold pressure, when blood flow returns to normal in damaged blood vessels. The integrated model can be used for blood pressure support biomedical devices. Ill. 9, bibl. 10 (in English; abstracts in English and Lithuanian).


Kuriant medicinines intelektualias elektronines monitoringo sistemą reikalingi fiziologinių sistemų modeliai. Pasiūlytas elektros grandinių pagrindu sukurtas veninės kraujo modelis gali būti panaudotas kuriand krauju spaudimo palaičymo realaus laiko įrenginius. Sukurtas veninės kraujo modelis tobulinamas Starlingo rezistoriaus modelio patobulinimas. Esami statiniai modeliai netinka, kai audinių spaudimas padidėja. Sukurtas dinaminis netiesinis modelis leidžia nustatyti spaudimo slenkstį, kai kraujo modelio kažkokia reikšmė atsiranda. Integruotų modelį galima naudoti biomediciniuiose kraujo spaudimo palaičyko įrenginiuose. Ill. 9, bibl. 10 (anglų kalba; santraukos anglų ir lietuvių k.).