

Article



Switching Ripple Harmonics Attenuation in DFIG and Matrix Converter-Based WECS

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Abstract: The analysis presented in this paper is focused on the harmonics distortion damping in the case of bidirectional power-flow of the electronics device-matrix converter as an interface between two power sources. Bidirectional energy flow takes place in the matrix converter that is used in renewables, hybrid transformers, microgrids, etc. It is observed that the matrix converter generates sinusoidal voltage with some amount of harmonic distortion and worsens in the quality of power in the utility grid. Taking into account the bi-directional energy flow and the matrix converter operation principle, four key requirements for the filters are formulated. Six theoretically possible filter topologies are investigated for compliance with these requirements. Two of the filter topologies are recognized as complying with these requirements and applicable for the switching ripple harmonics damping in the utility grid connected matrix converter in the case of bidirectional power flow. The suitability of these topologies was verified by MATLAB/Simulink simulation. Using the proper filter topology will significantly reduce the size, weight and cost of the components of the filter, as well as the utility grid's pollution by switching ripple harmonics. It is appropriate to apply such filters to matrix converters that operate in wind turbines installed in doubly fed induction generators. These filters should also be used in hybrid transformers and other high-power devices with matrix converters.

Keywords: AC-AC power converters; frequency converters; passive filters; harmonics

1. Introduction

Nowadays, with the high development of renewable energy sources, more and more power systems are characterized by large shares of resources interfaced with power electronics [1]. Wind energy generation has shown, and will continue to show, its vital presence in the upcoming years. Presently, the technology is moving towards variable speed wind energy conversion systems (WECS). Wind turbines equipped with doubly-fed induction generators (DFIG), which belong to variable speed WECS, have already proven their superiority over other configurations. DFIGs have many benefits and their competitive advantages make them the favorite choice for wind energy conversion systems that can be connected to power grids. The main advantage of the doubly-fed scheme over the singly-fed scheme is that the power converter required for the control of the machine can have a substantially reduced volt-ampere rating. Unlike other grid-connected renewable energy plants, the converter in the DFIG-based WECS provides bidirectional power-flow control, thereby enabling the DFIG to operate in either sub-synchronous or super-synchronous modes.

The use of power electronics technology in AC transmission systems is one of the pillars of the implementation of the flexible microgrid [2]. A hybrid distribution trans-

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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/). former is a potential cost effective solution to microgrid control devices. The hybrid distribution transformer is realized by augmenting a regular transformer with a fractionally rated power electronic converter, which provides the transformer with additional control capabilities. The hybrid distribution transformer can provide dynamic AC voltage regulation, phase angle control harmonic compensation and voltage sag compensation.

Currently, most of the wind power plants, hybrid transformers and microgrids are equipped with a two-stage back-to-back converter with DC link, which allows bidirectional power flow and converts the variable frequency voltage to the power grid frequency 50/60 Hz voltage [3]. However, in the DC link, large electrolytic capacitors are used, which are components with the shortest lifetime in comparison with any semiconductor element used in these converters. Furthermore, the presence of the electrolytic capacitors also increase maintenance costs of the power system components. Using converters without the DC link would reduce the maintenance costs, size, increase reliability and the operating life of the converters, as well as the whole renewable energy sources based power system.

In this paper, an application of the one-stage matrix converter (MC) is studied, since it provides some advantages such as:

- inherently bidirectional power flow—the one-stage MC can deliver or take power from the utility grid via direct conversion between input and output of the converter;
- the control modules of the MC are simpler than those needed by the two-stage power converters as both input current and output target voltages are modulated within the same algorithm;
- absence of limited operation time capacitors;
- distribution of the thermal stress in the commutation elements because of the high number of switches;
- higher maximum power density;
- higher maximum power to mass ratio.

The MC is capable of providing sinusoidal output voltages with varying amplitude and frequency, and sinusoidal input currents with adjustable power factor, irrespective of the load [4].

The MC is composed of nine semiconductor-based bidirectional switches. As presented in Figure 1, the MC could be used as an intermediate circuit between variable frequency source (consumer) of energy and constant frequency utility grid. Unlike other grid connected renewable energy plants, the matrix converter in the DFIG-based wind energy conversion systems provides bidirectional power-flow control, thereby enabling the DFIG to operate in either sub-synchronous or super-synchronous modes.



Figure 1. The diagram of the system researched in this paper.

The MC is a forced commutated converter that consists of nine bidirectional switches as the power elements to create a variable output voltage system. In contrast to the back-to-back converter, the MC contains no large energy storage elements (capacitors). The key element of the MC is the fully controlled four-quadrant bidirectional switch, which allows high-frequency operation. As presented in Figure 1, there are 27 possible combinations (vectors) for the bidirectional switches of this three-to-three phase matrix converter. With an MC, indirect space vector modulation (ISVM) can be applied to control output voltage and input current. The ISVM considers the MC to be of the indirect form of converter. It features a virtual voltage source inverter (VSI) control part, a current source rectifier (CSR) control part and a DC link in between. By using the ISVM strategy, the desired output voltage and input current are synthesized from the active vectors and zero vectors. As shown in Figure 2, the active vectors are formed from 18 possible switch combinations (-9, -8, ..., +8, +9) [5].



Figure 2. Graphic interpretation of bidirectional switch combinations: (a) sectors and direction of the output voltage vectors; (b) sectors and directions of the input line current vectors.

The two adjacent vectors approximate the space vector of the desired output line voltages and input currents. As presented in Equations (1) and (2), the frequency of the MC output voltage is determined by the angle *Qsc*, and the input current displacement is determined by the angle *Qsv*.

$$Q_{SC} = (\omega_i t - \varphi_{in}) + 30^\circ \tag{1}$$

$$-30^{\circ} \le \omega_i t - \varphi_{in} \le +30^{\circ} \tag{2}$$

where *t* is the time, determined through synchronization with the frequency of the power distribution lines, and φ_{in} is the preferred current displacement angle, which determines the reactive power at the area of input of the MC.

The control algorithm used for vector approximation is presented in Figure 3. According to the ISVM control strategy, it consists of two sequences representing the rectifier and inverter stages. Every sequence consists of sector determination and duty cycle determination. Both sequences are combined by the common duty cycle determination segment and bidirectional switchers control logic, as presented in Table 1.



Figure 3. Graphical interpretation of switcher's combination selection algorithm.

Table 1. Bidirectional switches combination logic.

	Output Voltage Vector Sectors SV						
	Sectors	1	2	3	4	5	6
Input current vector sectors SC	1	-7 +9 +1 -3	+9 -8 -3 +2	-8 +7 +2 -1	+7 –9 –1 +3	-9 +8 +3 -2	+8 -7 -2 +1
	2	+4 -6 -7 +9	-6 +5 +9 -8	+5 -4 -8 +7	-4 +6 +7 -9	+6 -5 -9 +8	-5 +4 +8 -7
	3	-1 +3 +4 -6	+3 -2 -6 +5	-2 +1 +5 -4	+1 -3 -4 +6	-3 +2 +6 -5	+2 -1 -5 +4
	4	+7 -9 -1 +3	-9 +8 +3 -2	+8 -7 -2 +1	-7 +9 +1 -3	+9 -2 -3 +2	-8 +7 +2 -1
	5	-4 +6 +7 -9	+6 -5 -9 +8	-5 +4 +8 -7	+4 -6 -7 +9	-6 +5 +9 -8	+5 -4 -8 +7
	6	+1 -3 -4 +6	-3 +2 +6 -5	+2 -1 -5 +4	-1 +3 +4 -5	+3 -2 -6 +5	-2 +1 +5 -4
Duty		daµ dav dβµ	dαμ dαυ dβμ	daµ dav dβµ	daµ dav dβµ	daµ dav dβµ	daµ dav dβµ
circles		dβυ	dβυ	dβυ	dβυ	dβυ	dβυ

One of the MC elements that has a major impact on the converter's performance is its input harmonic filter [6]. The MC voltage and current are sinusoidal just in case an effective filter is applied to suppress switching ripple harmonics. The possible filter options are shown in Figure 1. The selection of this filter configuration and its components' values is an important task that is neglected in many scientific works. The back-to-back converters traditionally used in energy systems with bidirectional power flow also have plug-in filters. However, the switching ripple harmonics generated by the back-to-back converters are significantly smaller than the switching ripple harmonics generated by the MC. This is related to the DC link in the back-to-back converters. Therefore, neither the back-to-back converters filter configurations nor their component values calculation methods are suitable for MC generated switching ripple harmonics filters. Until now, published papers have not provided studies on MC filters at bidirectional energy flow.

Therefore, the purpose of this research is to:

to analyze higher harmonic filter types proposed in the publications; to select filter configurations suitable for use in MC converters; to investigate the efficiency of these filters by way of simulation with bidirectional energy flow.

2. The Switching Ripple Harmonics of Matrix Converter

Grid power quality is one of the concerns in the converter interfaced systems. During the operation of grid-connected MCs, space vector modulation methods are commonly used to maintain the switching of the power semiconductor devices. The power semiconductor devices produce switching ripple harmonics, which can cause harmonic distortions and reduce power quality in the utility grid. An output voltage waveform of the MC and Fourier series components of harmonic spectrum in the case of an ideal voltage supply are presented in Figure 4. The uppermost harmonics of the MC current are around the switching frequency and repeated frequencies.





Some research works have been conducted on switching ripple harmonics damping. Various types of filters are recommended for use on MC-based electric drives. In addition to switching ripple harmonic attenuation, the filters also maintain integration and coupling connection between the utility grid and the MC.

Several filter types, namely, L, LC, LCL and LLCL, are presented in publication [7] concerning grid connection of converters for photovoltaic plants. Unlike photovoltaic plants, the converter in another renewable-energy-based power system, such as a double-fed induction generator-based wind energy conversion system, provides bidirectional power flow [8]. The filter for such power systems has to be designed to damp ripple harmonics in the case of the bidirectional power flow. Most power quality studies discussing grid-tied renewable-energy-based power systems are related to conventional DC-link back-to-back voltage converters [9]. For the ripple harmonics damping, in such a power system the first order L-type filter is usually proposed. In this case, the inductor L properly interacts with the DC-link storage capacitor, as presented in Figure 5a [10]. For novel one-



stage MC power systems, such interaction is impossible because of the absence of a DClink storage capacitor.

Figure 5. Single-line diagram of filter component connection: (**a**) in the conventional AC/DC/AC converter-based power system; (**b**) CL filter component connections in the utility grid line (grid side capacitor); (**c**) LC filter component connections in the utility grid line (grid side inductor); (**d**) LCL filter component connection in the DC/AC—utility grid system.

Only a few studies of harmonic distortions for the novel one-stage MC in bidirectional power flow system are published. The permissible level of harmonics for the integration of renewable energy power plants into the utility grid is defined in publication [11]. Publication [12] indicate that the level of harmonics when connecting a filterless MC to the utility grid does not meet the requirements of the grid codes. It should be noted that the interaction of the power distribution line parameters (induction, capacitance) with the filter components have not been addressed in the studies mentioned above. Some authors suggest using widely applicable first order or second order filters but do not examine the effect of filter parameters on harmonic distortions [13]. The efficiency of the filter directly depends on the filter element connection point. Some authors suggest inserting filter components into a circuit connecting the MC and the utility grid, others-circuitry that connects renewable energy power sources and the utility grid. The efficiency of a filter by damping the harmonics depends on the direction of the transmitted power and the harmonic flow direction. Figure 5b presents the CL filter component connection diagram applied in voltage-source and current-source converters [14]. The CL filter capacitor is on the utility grid side. By combining this arrangement, the damping of the switching ripple harmonics becomes ineffective if the MC operates in power consumption mode with respect to the utility grid. Figure 5c presents the LC filter component connection diagram proposed in publication [15]. The filter capacitor is on the MC side. Connecting this way, the filter capacitor will form a lower impedance path for the switching ripple harmonics if the MC is in the power supply mode with respect to the utility grid. This would increase the current in the capacitors circuit.

Figure 5d presents the LCL filter component connection diagram proposed in publication [16].

The LCL filter should block MC-generated switching ripple harmonics, protecting the utility grid from their access. If LCL filter component values were calculated incorrectly, this could lead to unwanted oscillations.

Figure 6 presents a two-branch filter component connection diagram proposed in publication [17].



Figure 6. Single-line diagram of two-branch filter component connection.

This type of filter has significantly higher component content than other filter topologies.

After reviewing a number of filter topologies, two main issues were raised:

Which filter topologies are suitable for switching ripple harmonics attenuation in the bidirectional power flow grid connected unit?

What is the influence of the utility grid parameters on filter attenuation characteristics?

These issues will be solved in further analysis.

3. Requirements for Switching Ripple Harmonics Filters

Some renewable energy devices, such as double-fed induction-generator-based wind power plants, can operate as energy consumers and as energy suppliers, depending on their operating mode. In such case, the MC must perform the bidirectional power transmission function and operate in both power consumption and power supply modes. In any of the above-mentioned modes, MC is the source of the switching ripple harmonics. To protect the utility grid from the MC-generated harmonics, the above-mentioned bidirectional power flow and operating modes must be taken into account.

The generation of higher frequency switching ripple harmonics is directly related to the principle of the MC operation, based on the power semiconductor devices switching. The filter designed for the utility grid protection from the above-mentioned harmonics must form a conduction path for the grid frequency voltage and prevent the passage of the harmonic frequency voltage. In the equivalent diagram shown in Figure 7, the MC is depicted as a harmonic frequency current source. If the renewable energy device is connected to the utility grid via an MC without the filter, the ripple harmonics generated by the MC will be directly transmitted to the grid. The filter maintaining integration and the coupling connection between the utility grid and the MC have to prevent the penetration of the harmonics current *I*_H into the grid.



Figure 7. A single-phase equivalent diagram of the power flow in the case of power consumption mode operating filterless MC.

The power flow direction in the supply operating mode and via filter equipped MC grid connected renewable energy device, is shown in Figure 8. In this case, the power flow direction coincides with the harmonics current direction. The filter elements shunt the harmonic current, resulting in a significantly lower amount of ripple harmonics.



Figure 8. A single-phase equivalent circuit diagram of the supply mode operating filter equipped MC.

The power flow direction in the consumption operating mode and via filter equipped MC grid connected renewable energy device, is shown in Figure 9. In this case, the power flow direction does not match the harmonics direction. The direction of the power flow has changed while the current direction of the harmonics remains the same. It follows that the same filter topology can be used to attenuate the harmonics.



Figure 9. A single-phase equivalent circuit diagram of the consumption mode operating filter equipped MC.

As can be seen from Figures 8 and 9, the MC operating in the power supply and power consumption modes can be considered as a source of harmonics. Regardless of the power flow direction, and in the same renewable energy device operation mode, the value of harmonic current *I*_H remains unchanged:

$$I_{InH} = I_H ; (3)$$

Since the generation of switching ripple harmonics is related to the principle of the MC operation, the filter must form the conduction path for the current I_{inH} and not interrupt the flow of I_{inH} ; otherwise the MC would not work properly because of the unlimited growth of ripple harmonics voltage V_{H} . As presented in Figures 8 and 9, the filter has to create the conduction path to neutral for I_{inH} with impedance lower than ZGRID. In addition, the level of V_{InH} must decrease less than V_{H} (Nomenclature):

$$V_{lnH} < V_H . (4)$$

In constructing a conduction path to neutral, the filter must prevent the ripple harmonics from penetrating the grid:

$$I_{outH} \ll I_{InH} \to 0. \tag{5}$$

The harmonics level in the input of the filterless MC is determined by the utility grid impedance Z_{GRID} (Figure 7).

$$\frac{V_H}{I_H} = Z_{Grid} ; (6)$$

The harmonics level in the input for the filter composed MC is determined by the filter impedance Z_{inF} (Figures 8 and 9).

$$\frac{V_{InH}}{I_{InH}} = Z_{inF} ; \tag{7}$$

The filter impedance has to be less or equal to the utility grid impedance:

$$Z_{inF} \le Z_{Grid} \to 0 \tag{8}$$

According to this, the filter input impedance is:

$$H_1(j\omega) = \frac{1}{Z_{InF}} \to \infty.$$
⁽⁹⁾

Furthermore, the filter input impedance for the frequency of the utility grid ω_s must be as high as possible:

$$H_1(j\omega) = \frac{I_{InH}}{V_{InH}} \to \infty; \tag{10}$$

$$H_1(j\omega) \gg H_1(j\omega_S); \tag{11}$$

The filter current transfer ratio $H_2(j\omega)$ must be as low as possible to conduct a current of utility grid frequency ω_s :

$$H_2(j\omega) = \frac{I_{OutH}}{I_{InH}} \to 0 \tag{12}$$

$$H_2(j\omega_S) = 1 \tag{13}$$

Based on the foregoing statements, these key requirements that the filter should meet in the MC-based bidirectional power flow implementing utility grid connected equipment, are formulated:

- the filter input impedance H₁(*j*ω) has to meet the requirements presented in Equations (10) and (11);
- the filter current transfer ratio $H_2(j\omega)$ has to meet the requirements presented in Equations (12) and (13.

4. Characteristics of the Most Commonly Used Filters

Several types of filters, namely, L, LCL and LC-type, are provided in the publications concerning bidirectional power flow implemented, grid connected voltage source inverters and back-to-back converters [18,19]. This paper examines the possibilities of using these types of filters to attenuate the ripple harmonics in the bidirectional power flow implemented utility grid connected MC. This is done by examining the frequency response of the filters, taking into account the nature of the MC-generated harmonics, and the bi-directional power flow through the MC.

4.1. L Filter Characteristics

As described in the reviewed study [18], a first order L-type filter operates as a filter interface between the converter, which is operating as an energy source and the utility grid, to smooth the ripple harmonics. Advantages, such as simple design and lower number of filter components, are shown. The inductor L properly interacts with the DC-link storage capacitor of the conventional DC link-based back-to back converter. In this paper, the L filter application in bidirectionally operating matrix converter for renewable energy application was studied. An absence of the DC-link storage capacitor in the MC complicates the situation. This interaction, which occurred using a conventional DC link-based back-to-back converter, is not possible in the case of the MC use. The single-phase equivalent circuit diagram of the three-phase grid-connected MC with an output L filter is presented in Figure 10, where L_F is the inductive filter component.



Figure 10. Single-phase equivalent diagram of the three-phase grid-tied MC with an output L filter.

The impedance of the filter is:

$$H_1(j\omega) = \frac{I_{InH}}{V_{InH}} = \frac{I_{InH}}{Z_{inf}I_{InH}} = \frac{1}{\omega(L_F + L_{TR} + L_{CB})} \ll \frac{1}{\omega_S(L_F + L_{TR} + L_{CB})}.$$
 (14)

The harmonics current attenuation is:

$$H_2(j\omega) = \frac{I_{OutH}}{I_{InH}} = 1 \gg 0.$$
(15)

Whether the L type filter meets the requirements that were formulated before can be determined by comparing the filter impedance to different frequencies—the impedance for an MC ripple harmonics frequency and impedance for the utility grid main frequency. The impedance of the L filter (14) for the MC ripple harmonics frequency is lower in comparison with the impedance for the frequency of the utility grid voltage. This indicates that the L filter does not meet the requirements for the impedance, which is given in Equation (11). As seen from Equation (17), according to the transfer rate, the L filter does not create a barrier and allows the MC-generated harmonics to penetrate the utility grid. This shows that the L filter does not meet the requirement given in Equation (12). The same conclusion can be drawn from the L filters frequency response shown in Figure 11. Based on these two findings, it can be stated that the L filter is **not applicable** for switching ripple harmonics damping in the bidirectionally operating MC.



Figure 11. Frequency response $H_2(j\omega)$ of the L filter.

4.2. LCL Filter Characteristic

Another filter topology is LCL, which has recently taken the place of the most conventional inverter application [19]. According to the studies, despite having smaller capacitance and inductance values in comparison with the aforementioned L filter, the LCL filter can attenuate the ripple harmonics more efficiently. Furthermore, the voltage drop stemming from the harmonics across the filter is smaller than in the L filter. Despite the earlier mentioned advantages, the LCL filter has some disadvantages in comparison with the L filter. These are risk of resonance occurrence, phase lag and system design complicacy.

The single-phase equivalent circuit diagram of the three-phase grid connected MC with an output LCL filter is presented in Figure 12, where *L*_{F1}, *L*_{F2} and *C*_F are the inductive and capacitive filter components.



Figure 12. Single-phase equivalent diagram of a three-phase grid-tied MC with an output LCL filter.

The impedance of the LCL filter can be calculated according to the equation:

$$H_1(j\omega) = \frac{I_{InH}}{V_{InH}} = \frac{I_{InH}}{Z_{inF}I_{InH}} = \frac{1}{Z_{inF}}.$$
(16)

An induction of the filter elements and the utility grid elements such as transformer, distribution lines and connection cables $L_1 = L_{F1}$; $L_2 = L_{F2} + L_{TR} + L_{CB}$ can be calculated accordingly:

$$Z_{inF} = j\omega L_1 + \frac{j\omega L_2 \cdot \frac{1}{j\omega C_F}}{j\omega L_2 + \frac{1}{j\omega C}} = j\omega L_1 + \frac{L_2}{j\omega L_2 C_F - \frac{1}{j\omega}} = j\omega L_1 - \frac{j\omega L_2}{\omega^2 L_2 C_F - 1}$$
(17)
$$= \frac{j\omega^3 L_1 L_2 C_F - j\omega (L_1 + L_2)}{\omega^2 L_2 C_F - 1}.$$

$$H_1(j\omega) = \frac{\omega^2 L_2 C - 1}{j\omega^3 L_1 L_2 C - j\omega(L_1 + L_2)} \ll \frac{\omega_s^2 L_2 C - 1}{j\omega_s^3 L_1 L_2 C - j\omega_s (L_1 + L_2)}.$$
(18)

The output-voltage-based frequency response can be calculated by:

$$H_3(j\omega) = \frac{I_{OutH}}{V_{InH}} = \frac{1}{j\omega(L_1 + L_2) - j\omega^3 L_1 L_2 C_F}.$$
(19)

The current transfer ratio can be calculated by:

$$H_2(j\omega) = \frac{H_3(j\omega)}{H_1(j\omega)} = \frac{I_{OutH}}{I_{InH}} = \frac{1}{1 - \omega^2 L_2 C_F} \ll \frac{1}{1 - \omega_s^2 L_2 C_F}.$$
 (20)

According to Equation (18), the impedance of the LCL filter depends strongly on the L_1 value. The input impedance of this filter for frequency of the harmonics drops down and the main reason for this is the value $\omega^3 L_1$ in denominator of the equation. This shows that the LCL filter does not meet the input impedance requirement presented by Equation (11).

As shown in Equation (20), the LCL filter transfer ratio $H_2(j\omega)$ decreases with the frequency of the MC-generated ripple harmonic frequencies. This indicates that the LCL filter meets the second requirement associated with the current transfer ratio.

Despite meeting the current transfer ratio requirement, the LCL filter is considered **not applicable** for switching ripple harmonics damping in the bidirectionally operating MC.

4.3. LC Filter Characteristic

Another topology for an inverter or back-to-back converter switching ripple filtering proposed in publication [20] is an LC filter. The capacitor is connected to the inductor to create a low impedance path at high frequency ripples.

The single-phase equivalent circuit diagram of the three-phase grid-connected MC with an output LC filter is presented in Figure 13, where L_F and C_F are the inductive and capacitive filter components.



Figure 13. A single-phase equivalent diagram of the three-phase grid-tied MC with an output.

As Equation (20) in the aforementioned LCL filter study shows, the current transfer ratio of the LCL does not depend on the inductor L_1 value. According to the key requirements the filter impedance should be as high as possible, $H_1(j\omega) \Rightarrow \max \Rightarrow \infty$. In this regard, the LC filter can be considered as a simplified LCL filter version. The MC operating in power consumption mode can be considered as a source of current that generates the high frequency switching ripple harmonics. Therefore, there is no necessity to limit the current across the filter capacitor *C* by the inductor L_1 . The impedance of the LCL filter in the case of $L_1 = 0$; $L_2 = L_{F2} + L_{TR} + L_{CB}$ is:

$$H_{1}(j\omega)_{L_{1}=0} = \frac{\omega^{2}L_{2}C_{F} - 1}{j\omega^{3}L_{1}L_{2}C - j\omega(L_{1} + L_{2})} = -\frac{\omega^{2}L_{2}C_{F} - 1}{j\omega L_{2}}$$

$$= \frac{j\omega L_{2}\left(\omega C_{F} - \frac{1}{\omega L_{2}}\right)}{\omega L_{2}}.$$
(21)

The values of the filter components are usually calculated based on the assumption that their operating frequency is significantly higher than the resonance frequency, $\omega \gg \omega_{\text{Res.}}$ Taking into account that $\omega C \gg \frac{1}{\omega L_2}$ and $\omega C_F - \frac{1}{\omega L_2} \approx \omega C_F$, the filter impedance is:

$$H_1(j\omega) \approx j\omega C_F \gg j\omega_S C_F. \tag{22}$$

As Equation (22) shows, the LC filter impedance for ripple frequencies is sufficiently higher in comparison with the impedance for the frequency of the utility grid voltage main harmonics. It means that the LC filter meets the input impedance requirements for the ripple harmonics damping described in (10) and (11).

The current transfer ratios of the LC filter are calculated by:

$$H_2(j\omega) = \frac{1}{1 - \omega^2 L_2 C_F}.$$
(23)

As Equation (23) shows, the LC filter meets the current transfer ratio requirement for the ripple harmonics damping described in (12) and (13).

Since both key requirements for the filters that were formulated before are met, it can be argued that the LC filter is **applicable** for switching ripple harmonics damping in the bidirectionally operating MC.

According to the LC filter frequency response $H_2(j\omega)$ presented in Figure 14, the LC filter transfer ratio is below the L filter transfer ratio in almost the entire frequency range,

except for the frequency area (10⁴–10⁵ Hz) in which the MC-generated harmonics concentrate. In this frequency range, the LC filter attenuates the MC-generated harmonics most effectively.



Figure 14. Frequency response $H_2(j\omega)$ of the LC filter.

Figure 15 shows the effect of the utility grid transformer impedance on the filter transfer ratio $H_2(j\omega)$. According to the frequency response, it is seen that the influence of the utility grid transformer impedance depends on the ratio of the transformer and the MC capacities. It is also seen that the maximum transfer ratio is achieved when the ratio of the transformer to the MC power is 100%. It means that the utility grid impedance as well as the power distribution line impedance can significantly increase the LC filter's ability to attenuate switching ripple harmonics.



Figure 15. The effect of the utility grid transformer impedance on the filter transfer ratio $H_2(j\omega)$.

4.4. Resonant Filter Characteristic

The application of the resonance filters to the attenuation of the MC-generated switching harmonics is rarely seen in publications. The resonance filter is analyzed only in publication [21]. According to this study, the resonant filter provides a very low impedance path and absorbs the high frequency harmonic currents. Regarding the frequency of the utility grid voltage, the resonant filter can act as a reactive power compensator.

The voltage resonant filter consists of a serial resonant circuit connected in parallel to a converter. The single-phase equivalent circuit diagram of the three-phase grid-connected MC with a voltage resonant filter is presented in Figure 16, where L_{F} , and C_{F} are the inductive and capacitive filter components.



Figure 16. A single-phase equivalent circuit diagram of the resonant filter component connection.

Component values in this type of filter are calculated to provide as little impedance Z_{RFIL} as possible. The nature of the Z_{RFIL} must be active. Theoretically, the $H_1(j\omega)$ of the voltage resonance filters is extremely small in the narrow frequency range. This means that the voltage-resonance filters are only intended to suppress the narrow-band harmonics. In Figure 17, the voltage resonance and the LC filter frequency responses are presented. When comparing the frequency response, it is seen that the voltage resonance filters are ineffective in suppressing harmonics that are above and below the resonant frequencies.

$$Z_{GRID} = j\omega L_{TR} + j\omega L_{CB} \tag{24}$$

$$Z_{RFIL} = j\omega L_F - \frac{j}{\omega C_F}$$
(25)

$$H_1(j\omega) = \frac{1}{Z_{RFIL} \parallel Z_{GRID}} = \frac{Z_{RFIL} + Z_{GRID}}{Z_{RFIL} \times Z_{net}} \to \infty$$
(26)

$$H_2(j\omega) = \frac{I_{OutH}}{I_{InH}} = \frac{I_{InH}}{I_{InH} \times \left(1 + \frac{Z_{net}}{Z_{fil}}\right)} = \frac{1}{\left(1 + \frac{Z_{net}}{Z_{fil}}\right)} \to 0$$
(27)



Figure 17. Frequency response $H_2(j\omega)$ of the voltage resonant filters.

As Equations (26) and (27) show, in the case of $Z_{\text{RFIL}} \rightarrow 0$, the voltage resonant filter meets the requirements described in (10) and (12). However, the requirements are only met in a special case of $Z_{\text{RFIL}} \rightarrow 0$, that is, only when the frequency range is very narrow and close to the resonant frequency ω_{RES} .

The voltage resonant filter is appropriate for damping the harmonics of frequencies relatively close to the frequencies of the electrical grid, it means k = 3rd, 5th and 7th harmonics. The frequency response of the resonant filter is sharp and upright and this filter is effective on harmonics with frequencies close to grid frequency f_s and higher k^*f_s . The MC-generated harmonics have a different spectrum of frequencies. As shown in the Fourier series (Figure 4), the MC input and output currents have a significantly higher frequency spectrum over the utility grid frequency: $f_s \leq f$, $H_1(j\omega_s) \ll H_1(j\omega)$. In addition to this, the spectrum is considerably wider. The resonant filter meets the requirements for a very narrow frequency range. As a result, the resonant filter is considered as **not applicable** for switching ripple harmonics damping in the bidirectionally operating MC.

4.5. Two-Branch Filter Characteristic

Publication [21] introduced one of the rarely applied filter topologies—the twobranch filter. This study evaluated a possibility of applying this topology to the bidirectionally operating MC. The single-phase equivalent circuit diagram of the three-phase grid-connected MC with a two-branch filter is presented in Figure 18, where L_2 , L_3 , L_5 , L_6 , R_2 , R_4 , R_6 , R_7 , and C_2 and C_5 are the active, inductive and capacitive filter components.



Figure 18. A single-phase equivalent diagram of a two-branch filter component connection.

A comparison of the frequency response $H_2(j\omega)$ of the two-branch filter with the frequency response $H_2(j\omega)$ of the previously analyzed LC filter was performed to evaluate its applicability. The same L and C values were maintained. Therefore, an equation sequence analysis was carried out.

The frequency response of the filter is calculated under the equation sequence:

$$H_{2}(j\omega) = \frac{I_{\text{outH}}(j\omega)}{I_{\text{InH}}(j\omega)} =$$
$$= \frac{Z_{d}(\omega)}{(Z_{l}(\omega) + Z_{b}(\omega) + Z_{d}(\omega))} \times \frac{Z_{l}(\omega)}{(Z_{a}(\omega) + Z_{c}(\omega))};$$
(28)

$$Z_{b1}(\omega) = \frac{R_2 j \omega L_2}{(R_2 + j \omega L_2)};$$
(29)

$$Z_{b2}(\omega) = R_3 + j\omega L_3; \tag{30}$$

$$Z_b(\omega) = \frac{Z_{b1}(\omega) \cdot Z_{b2}(\omega)}{Z_{b1}(\omega) + Z_{b2}(\omega)};$$
(31)

$$Z_{a1}(\omega) = \frac{R_7 j \omega L_5}{(R_7 + j \omega L_7)};$$
(32)

$$Z_{a2}(\omega) = R_6 + j\omega L_6; \tag{33}$$

$$Z_a(\omega) = \frac{Z_{a1}(\omega) \cdot Z_{a2}(\omega)}{Z_{a1}(\omega) + Z_{a2}(\omega)};$$
(34)

$$Z_c(\omega) = \frac{R_8 j \omega C_5}{R_8 + 1/(j \omega C_5)};$$
(35)

$$Z_{c2}(\omega) = \frac{1}{(j\omega C_2)};$$
(36)

$$Z_l(\omega) = R_l + j\omega L_l; \tag{37}$$

$$Z_{ac}(\omega) = Z_a(\omega) + Z_c(\omega); \qquad (38)$$

$$Z_d(\omega) = \frac{Z_{ac}(\omega) \cdot Z_{c2}(\omega)}{Z_{ac}(\omega) + Z_{c2}(\omega)};$$
(39)

Figure 19 shows a frequency response of the two filters. These are the two-branch filter and the LC filter. Due to the largest number of components, the two-branch filter components' L_2 , L_5 , C_2 and C_5 calculated values are significantly lower in comparison with the LC filter component L and C values. The two-branch filter component values are calculated based on the impedance and capacitance ratios $L_2 = L_5 = L/3$; $C_2 = C_5 = C/3$. The frequency responses show that the damping efficiency of the switching ripple harmonics of the carrier frequency 10⁴ Hz are almost equal for both the LC filter and the two-branch filter. For the higher frequencies, the current frequency response shows an advantage of the two-branch filters—the damping efficiency of this filter is higher in comparison with the LC filter. The application of the two-branch filter is determined only by the component weight and the price factor.



Figure 19. Frequency response $H_2(j\omega)$ of the two-branch filter.

Because all of the requirements for the ripple harmonics damping described in (8–11) are met, the two-branch filter is considered **applicable** for switching the ripple harmonics damping in bidirectionally operating MC for renewable applications.

5. Simulation Studies

The simulation was developed in Matlab/Simulink. The Matlab/Simulink model of the bidirectionally operating MC consists of four parts. The first part contains the utility grid and distribution lines components' simulation blocks—voltage source plus impedance of utility grid. The Matlab/Simulink block three-phase voltage source in series with RL branch was used to simulate these components. The second part contains blocks for filter element simulation (Figure 20). Matlab/Simulink blocks implementing a three-phase series RLC branch were used to simulate filter components. The "Branch type L "setting was selected to simulate the filter inductance. The "Branch type C" setting was selected to simulate the filter capacity.



Figure 20. The Matlab/Simulink components implementing utility grid, distribution lines and the filter.

The third part contains nine ideal bidirectional switches of the MC and space vector modulation control modules (Figure 21). To simulate the ideal bidirectional switches of the matrix converter, blocks were used that implement an IGBT device in parallel with a series RC snubber circuit. Standard Matlab/Simulink subsystems running Park and Clarke transformations were used to simulate the space vector modulation system. Using the standard logic and comparison blocks, the sector separation subsystem was implemented.



Figure 21. The Matlab/Simulink components implementing the ideal bidirectional switches.



The fourth part contains right side LC filter and renewable energy source (consumer) components (Figure 22). Matlab/Simulink blocks implementing a three-phase series RLC branch were used to simulate filter components.

Figure 22. The Matlab/Simulink components implementing energy consumption side elements.

According to IEEE recommended practices and requirements for harmonic control in electrical power systems, it is recommended to use filter component values such that the filter reduces *THD*₁ to 5 percent. The filter components' values were calculated according to these guidelines and the methodology described below, i.e., on the basis of MC power and voltage drop across the filter.

Most authors of the publication suggested calculating the capacitor value according to its reactive power at the utility grid frequency [21].

$$Q_F = 0.1 \div 0.2 P_{MC} \tag{40}$$

$$C_F = \frac{Q_F}{3V_S^2 \omega_S} \tag{41}$$

The calculation of the filter induction value is based on the consideration that the voltage drop in the LC filter inductor is about 5% of the grid voltage ($0.05 V_s$). According to this consideration:

$$I_{MC}\omega_S L_F = 0.05V_S \tag{42}$$

$$L_F = \frac{0.05\sqrt{3}V_S^2}{S_{MC}\omega_S} \tag{43}$$

The values of filter components: $C_F = 14.43 \times 10^{-5} \text{ F} L_F = 2.02 \times 10^{-4} \text{ H}$

The simulation was performed with LC, CL and two branches' filters whose component values were calculated according to the same methodology. The two branches' filter component values used in the simulation are such that the same reactive power and voltage drop across the filter as with the other filters is maintained. This allowed a correct comparison of the simulation results presented in the Table 2 and Figure 23.

Table 2. The Matlab/Simulink simulation results.

	Filter	Mode	THD IOutH, %	THD <i>V</i> _R , %	IOutH, A	Ir, A	Vs, V	$V_{\rm R},{ m V}$	P, MW
1	LC	Power consump- tion mode	6.73	3.49	119	139	575	483	0.166
2	CL	Power consump- tion mode	52.0	22.0		Out	of normal	range	
3	Two branches	Power consump- tion mode	5.94	3.05	123	140	575	496	0.166
4	LC	Power supply mode	7.57	9.72	195	226	575	490	-0.161
5	CL	Power supply mode	76.0	8.78	205	226	575	960	-0.162
6	Two branches	Power supply mode	4.93	5.95	123	142	575	491	-0.162





Figure 23. The time course of the current of MC connection to utility grid point in the case of: (**a**) LC filter in power consumption mode; (**b**) LC filter in power supply mode.

In the case of LC filter use in the power consumption mode, THD I_{OutH} and THD V_R are close to the levels permitted by the standards. The voltage V_R is maintained at normal level. The use of LC filter in the power consumption mode causes a significant drop in voltage V_R —the CL filter interferes with MC. In the case of LC filter use in the power supply mode, THD I_{OutH} and THD V_R slightly exceeds the value allowed by the standards. The use of a two-branches filter allows the switching ripple harmonics to be suppressed to the level permitted by the standards. When the switching ripples are suppressed in the filter input current (Figure 23), the component of the filter resonant frequency (approximately 1000 Hz) becomes visible. The use of CL filter in the power consumption mode causes significant rise in voltage V_R —the CL filter is a barrier to power transfer to the utility grid. The simulation results support the assumption that CL (as well as LCL) filters are not applicable for the bidirectionally operating MC.

6. Conclusions

In this study, the **four base requirements** that must be met by the filter applied for the switching ripple harmonics attenuation in the bidirectionally operating, utility grid connected MC, are formulated. These requirements are expressed in Equations (8)–(11). The verification for the suitability of the commonly used filters (L, LC and LCL), resonant filter, and two-branch filter according to these four requirements was performed.

Having evaluated the characteristics of the L filter, it has been found that the L filter does not meet the requirements for the bidirectional power flow. As a result, the L filter is considered to be not applicable for the bidirectionally operating MC.

After evaluating the characteristics of the LC filters, it is found that this filter meets the formulated requirements. In the case of a grid side inductor connection, the LC filter is considered to be applicable for the bidirectionally operating MC. If the capacitor is connected to the utility grid side, it is found that the CL filter does not meet the requirements for the bidirectional power flow. In this case, the CL filter is considered not applicable for the bidirectionally operating MC.

The LCL filter, which is most commonly used in renewable power plants connected to the utility grid via a voltage source inverter, does not meet the requirements of bidirectional power flow. Therefore, the LCL filter is considered to be not applicable for the bidirectionally operating MC.

The resonance filter meets the formulated requirements only by attenuating switching ripple harmonics with a very narrow spectrum of frequencies. Therefore, the resonant filter is considered to be not applicable for the bidirectionally operating MC.

Having evaluated the characteristics of the two-branch filter, it has been found that this filter meets the formulated requirements. Due to the higher number of elements than in the other filter topologies, this filter attenuates the switching ripple harmonics more efficiently. Therefore, the two branches filter is considered to be applicable for the bidirectionally operating MC.

The simulation results support the assumption that the LC filter and two branches' filter is suitable for the bidirectionally operating MC both in power supply and power consumption modes. The simulation results show that voltage and current harmonic distortions are close to the levels permitted by the electrical code. The simulation also supports the assumption that CL (as well as LCL) filters are not applicable for the bidirectionally operating MC because the filters (as well as LCL) interfere with MC.

The simulation results showed a slight increase of THD in the renewable source current in power supply mode when the LC filter is connected. This must be taken into account in the calculation of component values for bidirectional filters.

7. Discussion

The results show that the theoretical assumptions regarding the suitability of the filter for a bidirectional energy flow controlling matrix converter are fully confirmed by Matlab/Simulink simulation. THD remains at a similar level at bidirectional energy flow. The results of the study also show that the possibilities to choose different types of filters at the point of the matrix converter connection to power grid are limited, because only two filter configurations can possibly be used—LC and two-branch filters. Therefore, a higher IGBT switching frequency needs to be used to increase the filter efficiency and reduce THD. Another way to reduce THD is to significantly increase the values of the filter elements, but this would have a negative impact in terms of size, weight and price. Therefore, reducing THD in systems with high-power matrix converters (double-fed induction generator for wind energy conversion system) becomes a challenging task because there are few means to improve filter efficiency without increasing filter parameters, dimensions and cost. In the light of these findings, it is appropriate to investigate the performance of filters consisting of more than two branches in further studies. Preliminarily, **Author Contributions:** Conceptualization, G.S.; methodology, G.S.; software, G.P.; validation, G.S. and G.P.; formal analysis, G.S.; investigation, G.P. and G.S.; resources, G.P. and G.S.; writing—original draft preparation, G.P.; writing—review and editing, G.S.; visualization, G.P.; funding acquisition, G.P. All authors have read and agreed to the published version of the manuscript.

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Nomenclature

Abbreviations	Value			
Cf	Filter capacitance			
CFMAX	Maximum value of filter capacitance			
fн	Frequency of special harmonic			
fs	Utility grid frequency			
<i>f</i> sw	Commutation frequency of MC			
$H_1(j\omega)$	Input impedance of filter			
H2(jω)	Output current based transfer ratio of filter			
H3(jw)	Output voltage based transfer ratio of filter			
Ін	Harmonic current of filterless MC			
Імс	Current of the MC on grid frequency			
IInH	Current of the harmonic at the filter input			
IOutH	Current of the harmonic at the filter output			
Ir	Current of the renewable source of energy			
Lf	Inductivity of the filter component			
LCB	Inductivity of the utility grid			
Ltr	Inductivity of the power transformer winding			
Рмс	Power of the MC			
<i>S</i> _{MC}	Total power of the MC			
V_H	Total harmonic voltage of filterless MC			
V_{InH}	Harmonics voltage of MC at input of the filter			
$V_{\rm LF}$	Voltage of filter inductor			
Vr	Voltage of renewable element			
Vs	Utility grid voltage			
Zgrid	Utility grid impedance			
ZInF	Input impedance of the filter			
Zrfil	Series impedance of resonance filter			
$\omega_{ m Res}$	Resonant frequency			
$Q_{\rm F}$	Reactive power of input filter capacitance			

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